

# 108 Maximum Sum

Modified from UVA108

A problem that is simple to solve in one dimension is often much more difficult to solve in more than one dimension. Consider satisfying a boolean expression in conjunctive normal form in which each conjunct consists of exactly 3 disjuncts. This problem (3-SAT) is NP-complete. The problem 2-SAT is solved quite efficiently, however. In contrast, some problems belong to the same complexity class regardless of the dimensionality of the problem.

Given a 2-dimensional array of positive and negative integers, find the sub-rectangle with the largest sum. The sum of a rectangle is the sum of all the elements in that rectangle. In this problem the sub-rectangle with the largest sum is referred to as the *maximal sub-rectangle*.

A sub-rectangle is any contiguous sub-array of size  $1 \times 1$  or greater located within the whole array. As an example, the maximal sub-rectangle of the array:

```

    0  -2  -7  0
    9   2  -6  2
   -4   1  -4  1
   -1   8   0 -2

```

is in the lower-left-hand corner:

```

    9  2
   -4  1
   -1  8

```

and has the sum of 15.

## Input

The input consists of several test cases.

Each test case begins with a single positive integer  $N$  on a line by itself indicating the size of the square two dimensional array. This is followed by  $N^2$  integers separated by white-space (newlines and spaces). These  $N^2$  integers make up the array in row-major order (i.e., all numbers on the first row, left-to-right, then all numbers on the second row, left-to-right, etc.).  $N$  may be as large as 100. The numbers in the array will be in the range  $[-127, 127]$ . If  $N$  is equal to zero, it means that the input ends.

## Output

The output is the sum of the maximal sub-rectangle, each case in one line.

## Sample Input

```

4
0 -2 -7 0 9 2 -6 2
-4 1 -4 1 -1
8 0 -2
0

```

## Sample Output

```

15

```